

Modeling and Compensation of Multivariable Creep in multi-DOF Piezoelectric Actuators

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Abstract—The scope of this paper is the modeling, identification and compensation of multivariable creep in piezoelectric actuators. Based on the inverse multiplicative scheme, we propose an approach to model and reduce the creep when the actuators have multiple degrees of freedom. The approach is simple to compute and easy to implement. The experimental results demonstrate the efficiency of the proposed approach on piezoelectric actuators.

I. INTRODUCTION

Piezoelectric materials are very prized for the design of actuators particularly dedicated to micro and nan positioning. This recognition is due to the high resolution, high speed and high force density that they offer. Unfortunately, piezoelectric materials are prone to nonlinearities that make the actuators lose their accuracy. Among these nonlinearities, the creep is a phenomenon that appears at very low frequency where the accuracy is brought into play. The creep is defined as the drift appearing after the transient part when a constant input voltage is applied to the piezoelectric actuator (piezoactuator) (see Fig. 1).

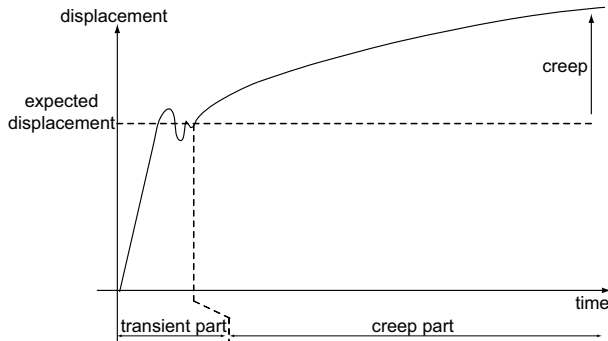


Fig. 1. Definition of the creep from a step response.

To remove the effects of the creep and to increase the accuracy of piezoactuators, closed-loop techniques (feedback) have been used [1]. These techniques also allow the consideration of the eventual model uncertainty or the parameters time dependence. However, feedback requires

the use of sensors that constitutes the main limitation for micro/nanopositioning applications. Indeed, while accurate and high bandwidth sensors are very expensive and with large sizes (eg. interferometer, optical sensors), those which are embeddable on the piezoactuators are very fragile and often sensitive to noise (eg. strain gages).

To surpass the limitation of closed-loop techniques in micro/nanopositioning, open-loop techniques (feedforward) have been used. In [2], *Jung et al.* uses a logarithmic function to model the creep phenomenon. To compensate it, an opposite logarithmic expression is established for the applied voltage such that the output displacement will remain constant. Another approach is to model the creep as the sum of several elementary linear first order recursive equations [3][4]. The compensation is therefore based on another recursive expression computed from the initial model. In [5], the creep is modelled by a continuous transfer function and its compensation is performed using the inverse model. The use of transfer functions is very interesting in an automatic point of view since the model parameters can be easily identified. However, directly inverting the model requires the bi-stability condition (ie. stability of the direct and of the inverse models). This is why in our previous work [6] we combine the model with a multiplicative structure to capture and compensate the creep phenomenon.

All of the above creep modeling and feedforward compensation apply for one-degree of freedom (DOF) piezoactuators, i.e. systems working on one axis. Notwithstanding, several developed piezoactuators possess multiple DOF in order to answer the requirement of several applications (x-y-z AFM scanning microscopy, 4-DOFs micromanipulation and microassembly, etc.). In these multi-DOFs piezoactuators, additionally to the creep of each axis, the coupling creep makes them very difficult to control. This paper presents the control of creep in piezoactuators that have several DOFs. Both the direct and the coupling creeps between axis are considered. Based on the modeling used in the previous work [6], we give an extension to consider multivariable creep and systems. Afterwards, we propose an identification procedure of the parameters and a multivariable compensator to delete the creep and the coupling. Finally, experiments on a real system validate the efficiency of the proposed technique.

The paper is organized as follows. In section-II, we remind the monovariate technique described in our previous work. In section-III, we present the proposed

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$$C_{i1}(s) = \frac{y_i^c(s)}{U_1(s)} \quad (7)$$

→ To identify K_{ij} and $C_{ij}(s)$ where $j \neq 1$, repeat the above sequence by applying the corresponding voltage U_j to the actuator.

C. Multivariable creep compensation

From the system's model as in (Eq 2), we derive the voltage to be applied that allows the output y meets the reference input $y^{ref} = (y_1^{ref} \ y_2^{ref} \ \dots \ y_n^{ref})^T$ as follows:

$$U(s) = (K + C(s))^{-1} y^{ref}(s) \quad (8)$$

After rearrangement of (Eq 2), the equation of the compensator becomes:

$$U(s) = K^{-1} (y^{ref} - C(s)U(s)) \quad (9)$$

Remark.2: in the particular case of monovariable system, the developed compensator defined in (Eq 9) (and therefore in (Eq 8)) gives the result in (Eq 3).

Remark.3: using the proposed compensator (Eq 9), both the direct creeps and the coupling creeps and coupling gains are deleted, i.e. the compensator performs the decoupling. Furthermore, the accuracy is improved because this compensator will result $y = y^{ref}$ when replacing U in (Eq 2) by (Eq 9).

Fig. 3 presents the block diagram of (Eq 9) which has an inverse multiplicative structure. The advantage is that there is no direct inversion of transfer $C(s)$ and therefore no need bi-causality condition is required for this matrix transfer function. It also means that non-invertibility condition to matrix $C(s)$ is necessary. In other words, systems without direct creep (i.e. $C_{ii}(s) = 0$) can also be considered by the compensator. We remind that K is invertible according to **Remark.1**.

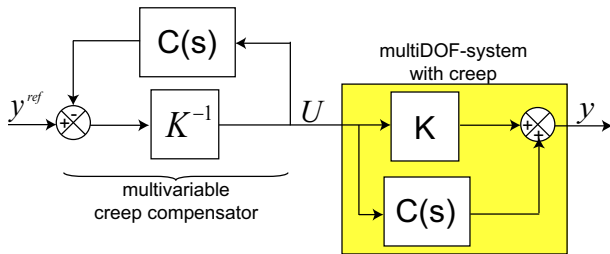


Fig. 3. Block diagram of the multivariable compensator.

IV. EXPERIMENTAL RESULTS

In this section, we apply the proposed method to model and compensate the creep of a 2-DOFs piezoactuator.

A. The experimental setup

The 2-DOFs piezoactuator, developed in [7], is made up of two piezolayers (PZT ceramic material) with 4 local electrodes at its surfaces and one middle electrode for ground (Fig. 4-a and b). It can be assimilated to a cantilever beam clamped at one end. The two DOFs are obtained with a judicious application of voltages on the electrodes. In the figure, P indicates the polarization direction of the material. The out-of-plane displacement y_1 is obtained by applying a voltage U_1 to the four electrodes (Fig. 4-c). To obtain the in-plane displacement y_2 , one has to apply a voltage U_2 and its opposite $-U_2$ to the four electrodes (Fig. 4-d). Finally the application of both U_1 and U_2 allows to obtain a displacement in the workspace (Fig. 4-e). The piezoactuator can therefore be seen as a system with input $U = (U_1 \ U_2)^T$ and output $y = (y_1 \ y_2)^T$.

The experimental setup is composed of (Fig. 4-f):

- the 2-DOF piezoactuator. Its total dimension is $15mm \times 2mm \times 0.5mm$,
- two optical sensors to measure the two displacements y_1 and y_2 at the tip of the piezoactuator. The sensors, from Keyence (LK2420), have $10nm$ of resolution and $0.1\mu m$ of accuracy.
- a computer and a DSPace-board to generate control signals, to implement the compensator and to acquire measurements. The chosen sampling frequency is $50Hz$ which is high enough to account the cutting frequency of the creep. The MATLAB-SIMULINK™ software is used to manage the signals and for the implementation.
- a custom high-voltage (HV) amplifier having two independant lines.

B. Characterization of the 2-DOF piezoactuator

In this subsection, we characterize the piezoactuator. For that, we first apply a step voltage $U_1 = 40V$ and set $U_2 = 0$. The resulting output y_1 and y_2 are represented in Fig. 5-a and c respectively. They clearly show the presence of the direct and coupling creeps due to U_1 . Then, we apply a step input voltage $U_2 = 40V$ and set $U_1 = 0$. As pictured in Fig. 5-b and d, the input voltage U_2 also causes a direct and a coupling creeps on y_2 and y_1 respectively. Now let us model the piezoactuator and identify the different parameters.

C. Modeling and identification

Using (Eq 2), the model of the 2-DOFs piezoactuator is:

$$\begin{pmatrix} y_1 \\ y_2 \end{pmatrix} = \left(\begin{pmatrix} K_{11} & K_{12} \\ K_{21} & K_{22} \end{pmatrix} + \begin{pmatrix} C_{11}(s) & C_{12}(s) \\ C_{21}(s) & C_{22}(s) \end{pmatrix} \right) \begin{pmatrix} U_1 \\ U_2 \end{pmatrix} \quad (10)$$

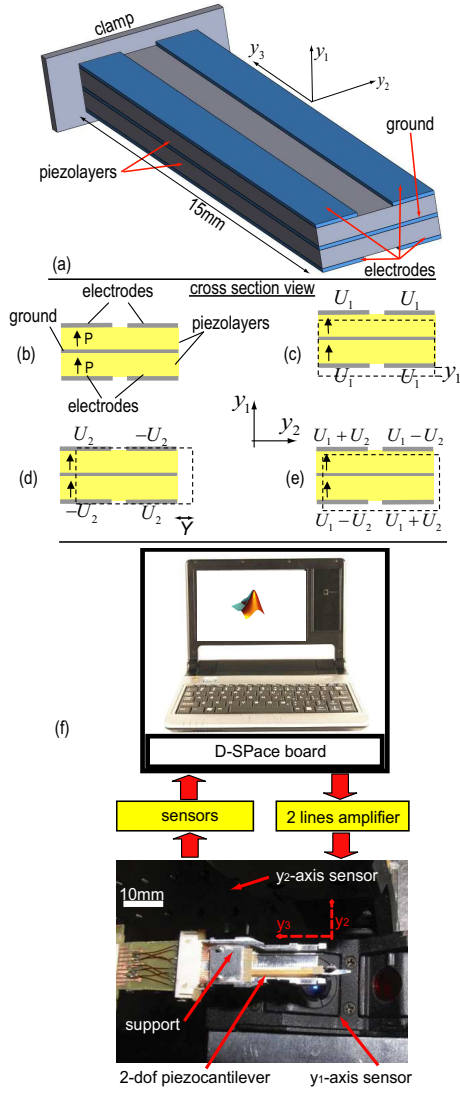


Fig. 4. (a) CAD view of the 2-DOFs piezoactuator [7]. (b) cross section view of the 2-DOFs piezoactuator. (c) achievement of y_1 displacements. (d) achievement of y_2 displacements. (e) achievement of both y_1 and y_2 displacements. (f) presentation of the experimental setup.

To identify K , we use the identification procedure in Section. III-B and the values after transient part issued from Fig. 5. These values are:

- the expected value $y_1^f = 59\mu\text{m}$ when applying $U_1 = 40\text{V}$ (Fig. 5-a),
- the coupling value $y_1^f = 3.56\mu\text{m}$ when applying $U_2 = 40\text{V}$ (Fig. 5-b),
- the coupling value $y_2^f = 4.28\mu\text{m}$ when applying $U_1 = 40\text{V}$ (Fig. 5-c),
- and the expected value $y_2^f = 27.8\mu\text{m}$ when applying $U_2 = 40\text{V}$ (Fig. 5-d),

We have:

$$K = \begin{pmatrix} 1.475 & 0.089 \\ 0.107 & 0.695 \end{pmatrix} \quad (11)$$

To identify the creep $C(s)$, we separate the creep

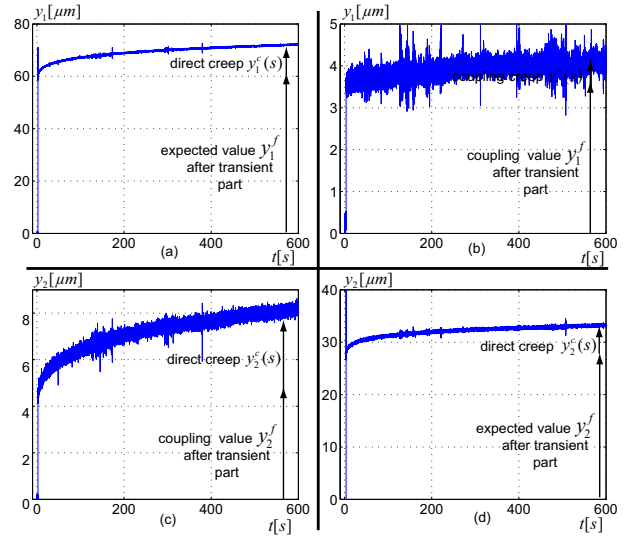


Fig. 5. Step response of the piezoactuator.

curves from Fig. 5 and we obtain the results pictured in Fig. 6.

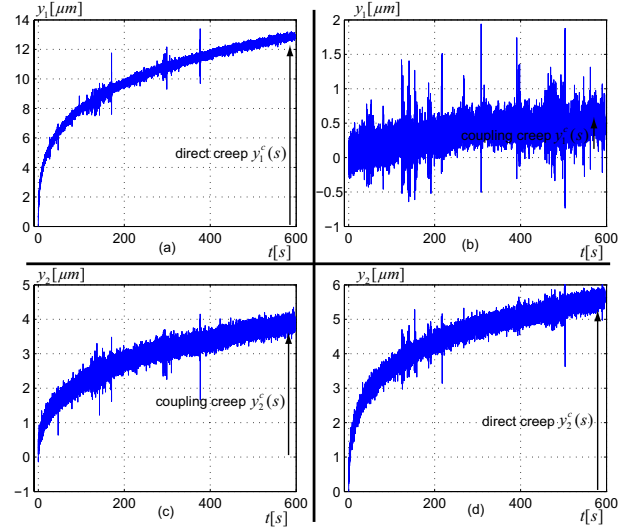


Fig. 6. Creep curves of the piezoactuator.

Then, following the creep identification procedure in Section. III-B, the different signals $y_1^c(t)$ and $y_2^c(t)$, and the ARMAX method (Autoregressive Moving Average eXogenous [8]), we obtain:

$$C(s) = \begin{pmatrix} \frac{3 \times 10^{-4} (s+50)(s+0.01)}{(s+0.12)(s+0.004)} & \frac{2 \times 10^{-6} (s+0.076)(s^2+78s+2599)}{(s+0.004)(s^2+4s+7.8)} \\ \frac{6.2 \times 10^{-5} (s+50)(s+0.011)}{(s+0.09)(s+0.003)} & \frac{1.4 \times 10^{-4} (s+50)(s+0.01)}{(s+0.12)(s+0.004)} \end{pmatrix} \quad (12)$$

Fig. 7 show the comparison of the simulation of the identified model with the experimental results. The figure show the convenience of the identified model.

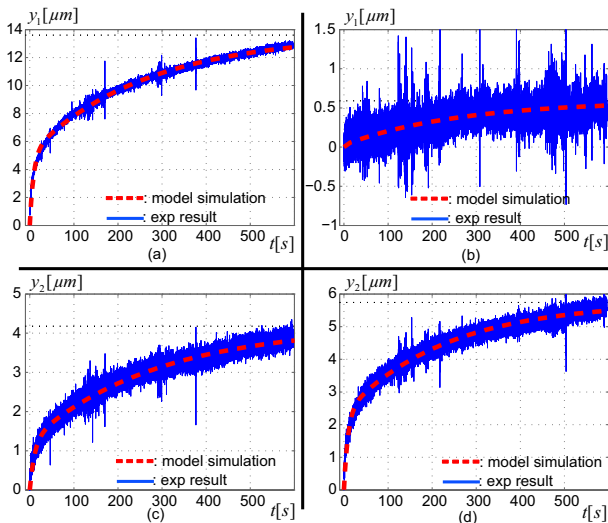


Fig. 7. Model simulation and experimental results for the creep.

D. Compensation of the creep

Let us now implement the creep compensator by using MATLAB-SIMULINK™ software. The implementation is based on the diagram shown in Fig. 3 and on the previously identified parameters.

First, we apply a step reference input $y_1^{ref} = 40\mu\text{m}$. Fig. 8-a pictures the resulting output y_1 . It clearly shows that the creep has been removed and we obtain the required accuracy: $y_1 = y_1^{ref}$. If we take a look on the output y_2 (see Fig. 8-c), we remark that not only the coupling creep is removed but also the whole coupling displacement (see **Remark.3**). Indeed, we have $y_2 = 0\mu\text{m}$ whatever y_1^{ref} non-null is.

Now, we apply a step reference input $y_2^{ref} = 20\mu\text{m}$. Once again, the creep has been removed and the accuracy was improved (Fig. 8-d): $y_2 = y_2^{ref}$. On the other hand, the coupling displacement and the coupling creep have also been removed because $y_1 = 0\mu\text{m}$ when y_2^{ref} is non-null.

V. CONCLUSION

This paper presented the modeling, identification and compensation of creep phenomenon in multi-DOF piezoactuators. The approach is an extension of the monovariable creep modeling and compensation presented in our previous work. An adapted identification procedure and a compensation scheme based on an inverse multiplicative scheme have therefore been proposed for the multivariable creep. The main advantages of the approach are the elimination of the creeps for every axis and the decoupling between these axis. Furthermore, the compensator is simple to compute and easy to implement since it is directly based on the identified model: as soon as the model is identified, the compensator is derived. Experimental results on a 2-DOFs piezoactuator have

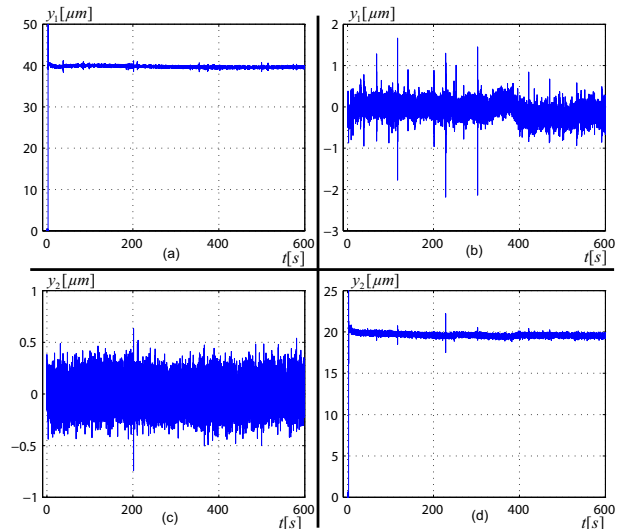


Fig. 8. Step response when using the creep compensator.

confirmed the efficiency of the proposed approach. Future works include the more in depth structural analysis of the compensator and its application to systems with higher DOFs, such as 3-DOFs piezotube actuator in atomic force microscopy.

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